Optimization of Computational Control-Parameter Values for Dynamic Optical Tomographic Image Reconstruction

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BACKGROUND and INTRODUCTION nt data, the issue of data integrity is particularly

ructed image accuracy to various types of data errors. Specific examples of some of the measurement-related issues that aris when data are collected using our group's previously described dynamic imager¹, for the case of a measurement on the forearm of a olunteer (Figure 1), are shown in Figure 2. Selected raw-data time series are plotted in each panel. The reduction in signal-to-nois atio (SNR) of the data with increasing distance between source and detector, that is illustrated in Fig. 2(a) points to the practical necessity for developing criteria for deciding which channels are excessively noisy and accordingly should be deleted from a data set. A second tial problem is the appearance of an appreciable difference between signals that are recorded by "conjugate" S-D channels (i.e., urce a, detector b vs. source b, detector a), which ought to be equal according to the principle of reciprocity2 (Fig. 2(b)). A third is the nces in scale between the data recorded in conjugate channels (Fig. 2(c)). Some of the observed differences can imply be attributed to the channels having different gain settings or DC offset levels, while in other cases they persist even after these nal factors are taken into account. These latte phenomena (among others not explicitly illustrated here) point to a ssity for developing criteria for deciding whether the data time series for each conjugate pair are sufficiently similar that the be regarded as "trustworthy."





on, obtained using the measurement geometri immetal protocol included two sets of Bour -trimental protocol included two sets of Bour -t's arm, with heating of the arm after the fit (a) are time-series recorded by channels w ⁰ (blue) and 13⁵ (red). The pairs of tracings) are time series recorded by two differe unels, both with 90° S-C-D angles. 2(b) and 2(c)

ntly are rou tely perfo ned in the setup stage of a tissue contact for all fibers, or to identify other instrumentational problems-and in the data pre-processing stage of our data analysis package³—as a post arement data integrity check-are computation of the coefficient of variation (CV) during the baseline period (first 400 seconds of data, in the example shown in Fig. 2) for each channel, application of a low-pass frequency filter to reduce noise a of the correlation coefficient (CC) and a normalized root mean squared difference1 (nRMSD) betw time series for all pairs of conjugate channels. Examples of the output of these computations, for the experiment that supplied the data hown in Fig. 2, are shown in Figure 3 for the 760 nm illumination wavelength that was used. (Qualitatively similar results were

tion wavelength, 830 (a obtained for the second illuminat nm.) It is seen that, as expected, low-pass filtering gnificantly impacts the CC and CV surfaces, while having a much smaller effect on the nRMSD results. The eration allows us to conclude, for example that the apparently poor reciprocity between conjugate airs with large S-C-D angles is principally a result of the low SNR of those time series, while the low reciprocity een between the S21+D22,S22+D21 conjugate pair is an ndication of a more serious problem

400 600 800 1000 1200

400 600 800 1000 1200 1600 1800 2000 Treatter

The image reconstruction step of the analysis ates two other essential features that are package incorp tely bound up, in practice, with issues of data integrity. First, the systems of equations that are solved uct the images are formulated by using the Normalized Difference Method4, which is robust to errors in the "initial guess." However, it is expected that its ince will be degraded by differences between ate channels of the type seen in Fig. 2(b), if these are too large. Second, truncated singular value tion (tSVD) is used as the solver/optimizer, in large part because it allows the user to fine-tune the of regularization by specifying the truncation point. Clearly needed, then, is a method for selecting the imal truncation point for a specified value of data SNR (or, conversely, for specifying the SNR required in

rder to allow one to retain the number of singular vectors necessary to successfully re resolution.) Similarly, the question of rigorous methods for choosing a threshold value for the low-pass filter, and CC, CV, and ins (above or below what level is a channel or conjugate pair of channels rejected?), all of which have an imp mage quality, must be addressed.

conjugate S-D chann of the time series re prior to low-pass filt thrachold of 0.15 Hz

Going beyond these practical consions, it is known that there are, at least in principle, defic particular data integrity indices we have employed. For example, a computed CC can be dramatically altered by the presence of even a small number of outliers in the data time series being compared⁵. An important limitation for all three indices is that they combine information from all frequencies into a single number. However, the number of data points in the time series we collect are too small to ion of useful frequency-dependent indices such as coherence, but significantly extending the data collection period is tot a viable option because (in addition of the practical issue of subject compliance) the requirement that the data be essentially stationary⁶ would almost certainly be violated. A worthwhile goal is to seek additional measures of data integrity that, when used in niunction with those already established, can be more informative and lead to more accurate decisions regarding which data to retain us strategies we are in the process of pursuing to accomplish the goals laid out above are described next.

STRATEGY 1: CHARACTERIZE SENSITIVITY of CC and nRMSD to KNOWN ERRORS

If, for example, the blue curves in Fig. 2 are discarded and replaced by identical copies of the corresponding red ones, then the CC and MSD are exactly 1.0 and 0.0, respectively. Then models for different types of mea ent error can be introduced in any degree and cos tion, and their effect on these measures of reciprocity precisely quantified. As a demonstration, this type of analysis was carried out using the data plotted as the red curve in Fig. 2(b) as the starting point, and incorporating four types of comm ttered measurement error: a constant difference (DC offset error), for which one unit was defined as the mean value of the stant ratio (Scale Factor); Additive Noise (Gaussian), for which one unit was defined as the sta deviation of the unperturbed time series: and Multiplicative Noise (Gaussian). Plotted in Figure 4 are surfaces illustrating the nce of CC on the magnitudes of both types of noise, and the dependence of nRMSD on the offset and scale errors. In each of these cases the two control parameters included in the plot are the ones to which the respective response variable is most sensitive while the remaining two are set to zero. Inspection of surfaces of these types allow us to determine what ranges of all modeled erro types are consistent with a CC value of at least, say, 0.8, or a nRMSD of at most, say, 0.3. (These specific values, which have vely been chosen as the acceptal ility thresholds for forearm me ment data, correspond to the red contours on the basep



Figure 4

odeled error types is ity of the CC and nRMSD with all four m ted in Figure 5, wl plotted against only one of the four control parameters, and each of the 125 data points (open diamond symbols) at each position along the abscissa is a CC (Fig. 5(a)) or a nRMSD (Fig. 5(b)) computed for one of the possible pe ns of the other three error types



scatter plot of all CC of all nRMSD values of the remaining three model error value, while the dotted lines pass

STRATEGY 2: SYNCHRONY INDEX COMPUTATION; DECISION TREE

The principal novelty here is that the set of data integrity indices already considered is augmented by the con ion of an additional one, i.e., the phase synchrony index7 (SI), a wavelet-based technique applicable to non-stationary time series. By convolving the nent time series for a conjugate pair of S-D channels with a scaled wavelet (the order-2 Coifman wavelet, sketched in Figure 6 was used here), only variations occurring on a time scale comparable to a frequency of interest are selected. The pair of time series obtained at each frequency scale are demodulated (i.e., their Hilbert

transforms are computed, the transforms are multiplied with a complex exponential having the ncy of interest, and the phase of the product is extracted), and the difference between the phases frequency of interest, and the phase of the product is extracted), and the difference between the phases of the two series is taken at all time points. The SI is a measure of the degree to which the phase difference useries much as a distance of the other of this is the set of the second VV difference varies over time. An illustration of the utility of this index is shown in Figure 7, where the difference varies over time. An initiatization 6 is use using or initia maximum of initial phase, and, starting at the 250-scored mark, a 500-point segment of one starting at the 250-scored mark, a 500-point segment of one starting at the 250-scored mark, as 500-point segment of one starting at the 250-scored mark, as 500-point segment of one starting at the 250-scored mark, as 500-point segment of one starting at the 250-scored mark as 500-scored mark

was substituted with a 90° phase-shifted copy of the other. It was predicted analytically that the SI central frequency (red), should be 0.6 for this situation, and the numerically computed SI plotted in the lower panel of Fig. 7 shows a rapid drop to near th should be 0.6 for this situation, and the nu predicted value after 250 seconds.

Comparison of a large set of SI values with the experimental time series from which they were derived have led to a tentative acceptance of 0.9 as a threshold value, below which data from conjugate S-D channels should be judged unequal, at the time scale(s) used in the SI computations. Illustrative examples drawn from experimental data and shown in Figure 8. In one case the SI is slightly greater than 0.9, and the differ ce between the phases of the two signals being compared is smaller than either of them, in terms of both magnitude and duration of the "blips" in Fig. 8(b). In the other case, 0.8 < SI < 0.9, and the difference between the phases is comparable in magnitude to those of the signals being compared



The second se

50 100 150 200 250 500 500 400 450



s of phase modulations (8(a),(c)) and phase modulation differences (8(b),(d)) ob ar conjugate pairs of S-D channels. For the example shown in 8(a),(b), the com tained from experimental data puted SI is 0.913; for the exan

ion of SI to the CC and nRMSD comp already performed allowed us to empiri shown in Figure 9, for the case of forearm measurements, that has two important uses. First (portions of Fig. 9 boxed in red), it can be incorporated into the software that controls the data acquisition process, for automatic flagging of S-D channels where poor fiber-skin contact is probable. Second, it can be incorporated into the data processing software package, to identify channels that should be ons on the grounds of failing to exhibit the expected degree of reciprocity



Figure 9. Empirically derived decision tree for determining which fibers have probable poor contact with skin during experim

rigorous answer to one of the remaining problems from the list set out above determination of an optimal value for low-pass filter thresholds. The idea is to conduct rapid (i.e., single-source) data collection, which will permit computation of SI values on much shorter time scales (i.e., out to higher frequencies) than is possible using full-tomographic measurement data. It is expected that, as shown as a sketch in Figure 10, the SI will decrease with increasing frequency, and that the frequency at which it begins to drop off rapidly will decrease with increasing S-C-D angle. The frequency at which the SI falls below 0.9 will be taken as an upper limit for the low-pass filter threshold for S-D channels having the corresponding angle.



STRATEGY 3: FINDING OPTIMAL TRUNCATION POINT for tSVD

ntical tomographic data set. it is useful to compare the temporal trend of the spatially averaged optical coefficient according to the re acted images to that obtained directly from the S-D channel data. An example of such a comparison, in this case carried out for a portion of a time series of data collected in a 3D optical mammography experiment, is shown in Figure 11. Here inse at the 760 nm measurement wavelength, averaged over all S-D channels, is plotted as a green curve, and the



ise in the reconstructed images, for the indicated numbers of singular vectors (SVs) included and a image pixels, are plotted as blue curves. It is clear from these results that retention of more than 100 SVs in the tSVD computation lity degradation. The degree of similarity between the shapes of the blue and green curves in Fig. 11 was qua intified by computing the RMSD between them; this difference is plotted vs. the number of SVs retained by the reconstruction algorithm, for ent wavelengths, in Figure 12. One possibly significant obse rvation is that the truncation point at which the RMSD ha its absolute minimum is different for the two wavelengths. In addition, these results have led us to expect that a generally useful (i.e. able to cases where no provocation is employed) strategy for finding the option point is to seek equal spatiotemporal variance between the detector and image data, as indicated by the conjectural sketch in Figure 13.



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(too few) Singular Vectors Re

A possible drawback of methods such as that just described is that the truncation point chosen by mir mizing a global spatial parameter could result in reconstructions that do not accurately recover properties of one or more localized regions. For this reason our intent is to use the variance equalization approach in combination with the previously described ability of our data analysis package to allow the user to visualize the right SVs of an imaging operator⁸, or weight matrix. In this way one can determine whether, for example, the number of SVs that equalizes image and detector variance are adequate for recovering information arising from the center (i.e., deep-lying part) of the imaging field.

mples of weight-matrix right SVs are shown in Figure 14, to illustrate some of the relevant co Figs. 14(a)-(e) were computed from an "unscaled" weight matrix, in which the sums of elements in some rows may be several orders of magnitude larger than the sums of elements in others. Almost all of the information in the most important SVs, i.e., those which correspond to the largest singular values (numbers in the upper right corners in Fig. 14 are the position of the displayed vectors in the rank-order list), is restricted to superficial regions of the medium. It is necessary to retain more than 100 SVs (Fig. 14(c),(e)) in order to ruct images that correctly locate information arising from the central region. In keeping such a large number, however, one trily also keeps those shown in Fig. 14(b),(d), as well as many others not shown, that allow high spatial frequency noise to affect the image quality. On the other hand, if the weight matrix is scaled so that all row sums are equal, then the number of SVs needed to allow recovery of information throughout the volume of the medium is much smaller (Fig. 14(f),(h),(j)), and the number that can admit noise into the image (Fig. 14(g).(i)) also is smaller



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An additional potential benefit of the SI is that it should allow us to derive a

